OCR Maths GCSE - Pythagoras

Q	Question		Answer	Marks	Part Marks and Guidance			
1	(a)		300 cos 30	2	allow 2 for 259.807611 rot to 1dp or more M1 for cos 30 = AD/300	or complete method using sin to find DB, then Pythag.		
	(b)		300 sin 30 or $\frac{BD}{300}$ = sin 30 DB = 149.6 to 150.1 DC = 329.6 to 330.1	M1 A1 A1	or 260 × tan 30 or $\sqrt{300^2 - 260^2}$ oe FT their DB, only if M1 earned	or using unrounded AD DB may have been found in (a), but allow credit for this in (b) only if it is clear that they know it is DB [image dim to include diagram and (a) below (b)]		
	(c)		308(.2)	4	Obtained from correct calculations M1 for attempt at using tan with <i>their</i> DC and 260 or their AD (or attempt at using cos with <i>their</i> BC and DC, following cos rule attempt) and M1 for inverse trig function seen or used A1 for ACD = 38.2()° or CAD = 51.7to 51.8°, with angle clearly identified; accept 38 or 52 for A1 if method seen allow B2 for 38.2()° or 51.7to 51.8°, with angle not clearly identified correctly; accept 38 or 52 with method seen	M0 for scale drawing or other correct trig fn following Pythagoras used		

2	(a)	567.5 to 567.6 or 568 or 570	3	nfww	570 from scale drawing scores 0
				M2 for $\sqrt{466^2 + 324^2}$ oe or equivalent complete method using trig (condone poor notation) Or M1 for $466^2 \pm 324^2$ or for 322 132 or any attempt at Pythagoras (eg 217 156 + 104 976)	
	(b)	More than 90 since diagonal should be less than 572 oe	1FT	FT only if at least M1 gained in (a)	

3		Correct perpendicular line	1	Within tolerance 88 to 92° of AB and within 1mm of D; line to reach at least from D to within 2mm of AB	
		Arcs showing compasses used correctly	1	As well as standard two pairs of two arcs, condone arc touching line drawn and radius drawn, condone 'kite construction'	'Kite construction' arcs through D, centre A, above and below AB intersecting with similar arcs centre B
					Also condone 'half kite' with just the intersecting arcs below AB but with radii AD and BD Ignore perp. bisector if also drawn
					NB 0 for spurious arcs drawn after the line – watch for these
		14.8 to 15.2	2	M1 for 7.4 to 7.6 [cm] or 1480 to 1520 [cm]	

4	(a)	$a^2 + 294^2 = 343^2$	M1	oe; for correct Pythagoras statement	allow M1 for $a^2 = 31213$
		$\sqrt{343^2 \pm 294^2}$	M1		
		176.6 to 177	A1	or B3 nfww; allow A1 for 180 if correct method seen	
	(b)	e.g. $\cos PLS = \frac{294}{343}$	M1	for a correct trig statement with clearly identified angle; may use their answer in (a); may find either angle in the triangle	Condone poor notation [S here is 3 rd vertex of triangle; candidates will use other refs, e.g. o, a and h marked on the triangle.]
		use of inverse trig function	M1	allow even if wrong trig function used	if e.g. 31 appears with no identification, allow this to imply the second M1
		bearing = 148.9 to 149.1	A2	A1 for LPS = 58.9 to 59.1 or for PLS = 30.9 to 31.1	allow 148.0 to 149.1 to imply the correct angle used

Question	Answer	Mark	Answer
5	179.8 to 180 with commentary (may be using letters)	6	e.g. : TG = 30/sin28 = 63.9 to 64 : TM = $\sqrt{(112^2 + 30^2)}$ =115.9 to 116 Allow fully correct alternative methods for TG and TM
	179.8 to 180 with no commentary	5-4	30/sin28 soi <u>and</u> √(112 ² + 30 ²) soi
	30/sin28 soi <u>OR</u> √(112 ² + 30 ²) soi <u>OR</u> sin 28 = 30/x <u>and</u> 112 ² + 30 ² soi	3-2	sin 28 = 30/x $\frac{OR}{112^2} + 30^2 soi$
	sin identified as the trig ratio required for TG oe $\frac{OR}{S}$ some use of Pythagoras for TM oe	1-0	No worthy work

6	2 × 10 ⁵ or 2.0 × 10 ⁵ or 1.96 ×	4	B3 for 195765 rot or 1.95765 × 10 ⁵ rot	
	10 ⁵ nfww		Seen Or M2 for $\sqrt{[(2.1 \times 10^5)^2 - (7.6 \times 10^4)^2]}$ oe Or M1 for $\pm (2.1 \times 10^5)^2 \pm (7.6 \times 10^4)^2$ soi	

7	$(x+2)^2 = 3^2 + x^2$ oe soi	M2	M1 for any combination of $(x + 2)^2$, 3^2 and x^2 in an equation	Condone omission of brackets for M2 or M1
	$x^{2} + 4x + 4$ oe 4x + 4 = 9 oe	B1 B1		
	1.25 or 1¼ or $\frac{5}{4}$	B1		

8		5.39	5	nfw B4 for other rot versions of 5.38516 nfww to at least 2dp	NB 0 for 5.4 without correct method seen – no marks for measuring
				OR M1 for 5 and 2 used or seen in right-angled triangle	eg 2 and 5 in relevant places on diagram or $\frac{1}{2} \times 5 \times 2$ or 5 + 2 = 7 or 5 across, 2 up seen
				M1 for an attempt at Pythagoras	eg <i>their</i> 5^2 and <i>their</i> 2^2 seen; second and third M1 s may be earned for an attempt at Pythag with a wrong triangle (possibly not right-angled)
				M1 for square root of (<i>their</i> $5^2 \pm their 2^2$) (may be implied by answer)	
				Allow A1 for 5.3 or 5.4 (dep on M3)	
				Following attempt at Pythagoras, allow B1 for <i>their</i> answer correctly rounded to 2dp if answer with more dp seen	

9	9.5()	4	nfww	0 for scale drawing
			M1 for $42^2 = 20.4^2 + w^2$ or other correct Pythagoras statement M1 for $\sqrt{42^2 \pm 20.4^2}$ If at least M1 earned, allow B1 for final answer FT <i>their</i> width – 27.2 Allow B3 for 36.7()	

10	3.2()	3	nfww M1 for 2.57 ² + 1.93 ² or 10.3(298) M1 for $\sqrt{2.57^2 \pm 1.93^2}$ oe	Or 6.6049 + 3.7249 Or M2 for equivalent complete method using trig (condone poor notation)
				3.2 from scale drawing scores 0

11	(a)	(i)	Using right-angled triangle with hyp 48 and side 42	M1	Just seeing marked on diagram is not sufficient	For a scale drawing, only this first mark is available
			$\sqrt{48^2 - 42^2}$ or 23.2()	M2	M1 for $48^2 - 42^2$ or for $\sqrt{48^2 + 42^2}$	
			11.76() or 11.8	A1		
		(ii)	sin C = 42/48	M1	Or equiv trig fns using <i>their</i> (a)	0 for scale drawing
			Inv trig fn seen or used	M1	Not dep on first M1	
			61 to 61.1	A1		
	(b)		[<i>d</i> =] 31/cos 25	M2	M1 for cos 25 = 31/ <i>d</i> or <i>d</i> × cos 25 = 31	may use sine with 65 or their (180 –
			34.2()	A1	Accept 34 with clear evidence of method	90 – 25) or tan and Pythagoras
						M0 for scale drawing

12	(a)	(i) 221 to 4	1		
		(ii) At lea ne side of AB, BC, CA measured accurately (11 cm, 9 cm, 8 cm with tolerance ±1 mm)	M1	May be implied by conversion to actual distances in cm, m or km (e.g. figs 275, 225, 2)	Often seen by diagram; may be implied by 28 e.g. 2.75 [km] seen by diagram earns first and third M1 s If only 8 seen must be clearly identified as AC
		Total distance found e.g. 28 cm on map or 700 000 cm soi	M1	FT <i>their</i> measurements; may be done after conversion	Figs 7 imply this second M1
		100 cm = 1 m and 1000 m = 1 km or 4 cm to 1 km soi	M1	May be earned earlier; need not be explicit M0 for e.g. 10 000 m = 1 km stated	May be implied by correct answer
		7 [km] and appropriate comment	B1	Accept 6.9 to 7.1 km and 'so OK', 'no, paths may be not straight so they have to go further' etc	E.g. if measurements or 28 not seen, may earn M0 M1 M1 B1
	(b)	1.41(4) Suitable comment e.g. '1.4 would be more accurate' or 'not too far out for a rough guide' or '1.5 is near and is easier for an estimate' or 'they have rounded	2	M1 for $1^2 + 1^2$ or $\sqrt{2}$ oe soi Allow A1 for 1.4 if M1 earned Allow SC1 for $1.5^2 - 1^2 = 1.25$ followed by $\sqrt{1.25} = 1.1(18)$ rot [can also earn comment mark following this] Dependent on answer 1.4 to 1.42 or Pythagoras attempted	Condone trigonometry used if correct answer obtained M0 for just 1 + 1 [= 2] with no evidence of squaring or square root Mark equivalently for other squares used e.g. M1 for $2^2 + 2^2$ and A1 for 2.82(8) and B1 for comparison with 3
		for an estimate' or 'they have rounded wrongly it should be 1.4 not 1.5'			

(c)	400	M1	Alternative method	
(0)	$\tan x = \frac{400}{600}$		M2 for vertical = 600 × tan40	
	Inverse trig function seen or used	М1	Or M1 for $\tan 40 = \frac{\text{vertical}}{600}$ or equivalents with horizontal distance AND A1 for vertical = 503(.45) or horizontal = 476(.7) and appropriate comment	Second M1 is independent of first – is earned for some indication that an inverse trig fn is needed to find an angle – even if done wrongly Comparison of tan 40 with tan <i>x</i> , both evaluated with appropriate comment earns full marks
	33.6 to 33.823 and appropriate comment e.g. not as steep as Mike thought	A1	Allow B3 for 33.6 to 33.823 or better and appropriate comment	Allow A1 for any of the following oe: "Good estimate - only 6° out" "Not a good estimate as it is 6° out " "Not far off, but 30° would have been closer" Condone 'so OK' etc

13	(a)	16.2 to 16.3	3	nfww	
				M2 for AP = $\frac{50}{\tan 72}$ or 50 × tan(90 – 72) Or M1 for tan 72 = $\frac{50}{AP}$ or tan(90 – 72) = $\frac{AP}{50}$	Or M2 for $AP = \frac{50 \sin 18}{\sin 72}$ or for complete correct method using sin or cos and Pythagoras Or M1 for $\frac{50}{\sin 72} = \frac{AP}{\sin 18}$
				SC1 only for 16.2 or 16.3 from scale drawing	
	(b)	[0]77.7 to [0]77.82	3	nfww M1 for $\tan APC = \frac{75}{their AP}$	Allow M1 for $tan ACP = \frac{theirAP}{75}$ provided angle is clearly indicated
				M1 for inverse trig fn soi If M2 earned, allow A1 for [0]78	eg invsin seen earns M0M1 0 for scale drawing
					Ŭ